

Candidate's Name in CAPITAL letters

Sec.

Branch

Roll No. :

Candidate's Signature

Invigilator's Signature

Date :

INSTRUCTIONS FOR OMR SHEET:-

1. Attempt ALL the questions.
2. Use only black or blue (ball pen) for darkening/writing in appropriate oval/box.
3. While darkening the oval/box it is to be ensured that these are darkened completely.
4. OMR sheet shall not be folded or tampered in any way.
5. Over writing/erasing/dual data & use of correction fluid will render OMR sheet invalid.

Time : 2 Hrs.

M.M. : 100

MATHEMATICS

Attempt each of questions :

1. If A and B be two sets containing 3 and 6 elements respectively, then the maximum number of elements in $A \cup B$ is
 a) 6 b) 3
 c) 9 d) 8
2. If $S = \{x : x \text{ is a positive multiple of 3 less than } 100\}$, $P = \{x : x \text{ is a prime number less than } 20\}$. Then $n(S) + n(P)$ is :
 a) 34 b) 31
 c) 33 d) 30
3. A set is a :
 a) Collection of well defined objects
 b) Collection of numbers
 c) Well defined collection of objects
 d) None of these
4. If $A = \{1, 2, 3, 4, 5, 6, 7\}$; $B = \{7, 8, 9, 10\}$ then $A - B =$
 a) $\{7, 9\}$ b) $\{3, 4, 8, 10\}$
 c) $\{7\}$ d) None of these
5. If $A = \{(x, y) : y = e^x, x \in R\}$ and $B = \{(x, y) : y = e^{-x}, x \in R\}$; then $A \cap B$
 a) $\{(1, 0)\}$
 b) $\{(0, 1)\}$
 c) $\{(1, 0), (0, 1)\}$
 d) ϕ
6. If $f(x) = 5 - 3x$ and $g(x) = 12x + 2$, which statement is NOT true?
 a) $f(0) > g(0)$
 b) $g(5) > f(5)$
 c) $f(1) > g(1)$
 d) $f(-1) > g(-1)$

Space for rough work

7. Let $A = \{x, y, z\}$ and $B = \{a, b, c, d\}$. Which one of the following is not a relation from A to B?
- $\{(x, a), (x, c)\}$
 - $\{(y, c), (y, d)\}$
 - $\{(z, a), (z, d)\}$
 - $\{(z, b), (y, b), (a, d)\}$
8. If $n(A) = 2$ and total number of possible relations from set A to set B is 1024, then $n(B)$ is :
- 5
 - 20
 - 10
 - 512
9. The domain of the function $f: \mathbb{R} \rightarrow \mathbb{R}$ defined by $f(x) = \sqrt{x^2 - 7x + 12}$ is :
- $(-\infty, 3] \cup [4, \infty)$
 - $(-\infty, 3] \cap [4, \infty)$
 - $(\infty, 3] \cup [4, \infty)$
 - $(3, 4)$
10. If S is a set with 10 elements and $A = \{(x, y) : x, y \in S, x \neq y\}$, then the numbers of elements in A is :
- 100
 - 90
 - 80
 - 150
11. If set A has 2 elements and set B has 4 elements then how many relations are possible from A to B ?
- 32
 - 128
 - 256
 - 64
12. The domain of the function f defined by $f(x) = \log(5 - 6x)$ is :
- $(-\infty, \frac{5}{6})$
 - $(\frac{5}{6}, \infty)$
 - $(-\infty, \frac{5}{6}]$
 - $[\frac{5}{6}, \infty)$
13. Let $A = \{3, 5\}$ and $B = \{7, 11\}$ and R be the relation from A to B defined and $R = \{(A, b) : a \in A, b \in B, a - b \text{ is odd}\}$, then
- $R = A \times B$
 - $R = \emptyset$
 - $R \subset A \times B$
 - $R \subset B \times A$
14. The range of function $f(x) = \sqrt{x-1}$ is :
- $(0, \infty)$
 - $[0, \infty)$
 - $[1, \infty)$
 - $(1, \infty)$
15. Let $A = \{x \in \mathbb{R} : x \neq 0, -4 \leq x \leq 4\}$ and $f: A \rightarrow \mathbb{R}$ be defined by $f(x) = \frac{|x|}{x}$ for $x \in A$ then A is :
- $\{1, -1\}$
 - $\{x : 0 \leq x \leq 4\}$
 - $\{1\}$
 - $\{x : -4 \leq x \leq 0\}$
16. $\cot(270^\circ + x) \cdot \cos(360^\circ - x)$ is equal to :
- $\sin x$
 - $-\sin x$
 - $\tan x$
 - $-\tan x$
17. $\cos(-1710^\circ)$ is :
- $-\sqrt{2}$
 - 1
 - 0
 - 1
18. The period of function $\cos 3x$:
- π
 - $\frac{\pi}{3}$
 - 2π
 - $\frac{2\pi}{3}$
19. In any triangle ABC, $\tan \frac{B+C-A}{2}$ is equal to :
- $\cot A$
 - $-\cot A$
 - $\tan A$
 - $-\frac{1}{2} \tan A$
20. If $\theta + \phi = \frac{\pi}{2}$ then value of $(1 + \tan \theta)(1 + \tan \phi) =$
- 2
 - 2
 - 1
 - 1
21. If $\sin \theta = \frac{3}{5}$, $\cos \phi = -\frac{12}{13}$, where θ and ϕ both lie in second quadrant, then the value of $\sin(\theta + \phi) = ?$
- $-\frac{20}{65}$
 - $-\frac{36}{65}$
 - $-\frac{56}{65}$
 - $\frac{56}{65}$

22. The expression $\frac{\sin(x+y)}{\sin(x-y)}$ is equal to :
- $\frac{\tan x + \tan y}{\tan x - \tan y}$
 - $\frac{\tan x - \tan y}{\tan x + \tan y}$
 - 1
 - 1
23. If $\sin x + \sin y = a$ and $\cos x + \cos y = b$ then the value of $\tan \frac{x+y}{2}$ is :
- $-\frac{a}{b}$
 - $\frac{a}{b}$
 - $\frac{b}{a}$
 - $-\frac{b}{a}$
24. $\sin 51^\circ + \cos 81^\circ$ is equal to :
- $\sin 19^\circ$
 - 0
 - $\sin 21^\circ$
 - $\cos 21^\circ$
25. If $\tan x = \frac{3}{4}$; $\pi < x < \frac{3\pi}{2}$ then value of $\sin \frac{x}{2}$ is :
- $\frac{3}{\sqrt{10}}$
 - $-\frac{3}{\sqrt{10}}$
 - $\frac{1}{\sqrt{10}}$
 - none of these
26. If $\sec \theta + \cos \theta = 2$, then value of $\sec^2 \theta + \operatorname{cosec} \theta$ is :
- 1
 - 2
 - 3
 - 4
27. In a circle of diameter 40 cm, the length of a chord is 20 cm. Then length of minor arc of the circle is :
- $10\pi/3$ cm
 - $20\pi/3$ cm
 - $20\pi/5$ cm
 - $6\pi/5$ cm
28. Let $\cos(\alpha + \beta) = \frac{4}{5}$ and $\sin(\alpha - \beta) = \frac{5}{13}$, where $0 \leq \alpha, \beta \leq \frac{\pi}{4}$, then $\tan 2\alpha =$
- $\frac{25}{16}$
 - $\frac{56}{33}$
 - $\frac{19}{12}$
 - $\frac{20}{7}$
29. The value of $\sin^2(15^\circ + x) - \sin^2(15^\circ - x) =$
- $-\frac{1}{2} \cos 2x$
 - 0
 - $\frac{1}{2} \cos 2x$
 - $\frac{1}{2} \sin 2x$
30. If for real values of x , $\cos \theta = x + \frac{1}{x}$, then
- θ is an acute angle
 - θ is right angle
 - No value of θ is possible
 - θ is an obtuse angle
31. The value of $(-\sqrt{-1})^{4n-3}$, where $x \in \mathbb{N}$ is :
- i
 - i
 - 1
 - 1
32. The smallest positive integer n for which $(1+i)^{2n} - (1-i)^{2n} =$
- 1
 - 2
 - 3
 - none of these
33. $|z_1 + z_2| = |z_1| + |z_2|$ is possible, if
- $z_2 = \bar{z}_1$
 - $z_2 = \frac{1}{z_1}$
 - $|z_1| = |z_2|$
 - none of these

34. If $x, y \in \mathbb{R}$, then $x + iy$ is a non-real complex number, if
- a) $x = 0$ b) $y = 0$
 c) $x \neq 0$ d) $y \neq 0$
35. If $z = x + iy$ lies in the third quadrant, then $\frac{\bar{z}}{z}$ also lies in the third quadrant if:
- a) $x > y > 0$ b) $x < y < 0$
 c) $y < x < 0$ d) $y > x > 0$
36. A real value of x satisfies the equation $\frac{3-4ix}{3+4ix} = \alpha - i\beta$, $\alpha, \beta \in \mathbb{R}$ if $\alpha^2 + \beta^2$ is:
- a) 1 b) -1
 c) 2 d) -2
37. The complex number z which satisfies the condition $\left| \frac{i+z}{i-z} \right| = 1$ lies on
- a) $x^2 + y^2 = 1$ b) the x-axis
 c) the y-axis d) $x + y = 1$
38. The imaginary part of $\frac{1-i}{1+i}$ is:
- a) 0 b) 1
 c) -1 d) $\sqrt{2}$
39. If $x + iy = (1+i)(1+2i)(1+3i)$, then $x^2 + y^2$ equals:
- a) -1 b) 0
 c) 1 d) 80
40. The square of $\frac{i}{1+i}$ in the form of $x + iy$ is:
- a) $0 + \frac{1}{2}i$ b) $\frac{1}{2} + 0i$
 c) $0 + \sqrt{2}i$ d) $0 - \frac{1}{2}i$
41. If $\frac{|x-4|}{x-4} > 0$ then:
- a) $x \in [4, \infty)$ b) $x \in (4, \infty)$
 c) $x \in (-\infty, 4)$ d) $x \in (-\infty, 4]$
42. If $|z+4| \leq 9$, then the maximum value of $|z+1|$ is:
- a) 10 b) 6
 c) 0 d) 4
43. Pairs of consecutive positive integers, both of which are larger than 5 such that their sum is less than 23 are:
- a) (6, 8), (8, 10)
 b) (8, 10), (10, 12)
 c) (6, 8), (8, 10), (10, 12)
 d) (6, 8), (10, 12)
44. The solution set of $\left| \frac{1}{x} - 2 \right| < 4$ is:
- a) $\left(-\infty, -\frac{1}{2} \right) \cup \left(\frac{1}{6}, \infty \right)$
 b) $\left(-\infty, \frac{1}{2} \right) \cup \left(\frac{1}{6}, \infty \right)$
 c) $\left(\frac{1}{6}, \infty \right)$
 d) $\left(-\infty, -\frac{1}{2} \right)$
45. The length of a rectangle is three times the breadth. If the minimum perimeter of the rectangle is 160 cm then:
- a) breadth > 20 cm
 b) length < 20 cm
 c) breadth ≥ 20 cm
 d) length ≤ 20 cm
46. The minimum value of the expression $3^x + 3^{1-x}$, $x \in \mathbb{R}$ is:
- a) 0 b) $\frac{1}{3}$
 c) 3 d) $2\sqrt{3}$

47. The third term of G.P. is 4. the product of its first 5 terms is:
 a) 4^3 b) 4^4
 c) 4^5 d) none of these
48. For a, b, c to be in G.P. the value of $\frac{a-b}{b-c}$ is equal to :
 a) $\frac{a}{b}$
 b) $\frac{b}{c}$
 c) both (a) and (b)
 d) none of these
49. If $a^x = b^y = c^z$ and a, b, c are in G.P., then x, y, z are in :
 a) A.P. b) G.P.
 c) H.P. d) None of these
50. a, b, c, d, e, f are in A.P. then e - c is equal to :
 a) $2(c - a)$ b) $2(f - d)$
 c) $d - e$ d) $2(d - c)$
51. t_6 of the sequence 2, 8, $\frac{16}{3}$,, is
 a) $\frac{81}{128}$ b) $\frac{128}{81}$
 c) $\frac{9}{5}$ d) $\frac{3}{2}$
52. The arithmetic mean of two numbers x and y is 3 and geometric mean is 1. Then $x^2 + y^2$ is equal to :
 a) 30 b) 31
 c) 32 d) 34
53. If $\frac{2}{3} = \left(x - \frac{1}{y}\right) + \left(x^2 - \frac{1}{y^2}\right) + \dots$ to ∞ and $xy = 2$, then the values of x and y? with the condition $x < 1$:
 a) $x = \frac{1}{2}, y = 4$ b) $x = \frac{1}{3}, y = 6$
 c) $x = 2, y = \frac{1}{4}$ d) none of these
54. The two geometric means between the numbers 1 and 64 are :
 a) 1 and 64 b) 4 and 64
 c) 2 and 16 d) 8 and 16
55. The nth term of a G.P. is 128 and the sum of its n-terms is 225. If its common ratio is 2, then the first term is :
 a) 1 b) 3
 c) 8 d) none of these
56. If the centroid of a triangle formed by the points (a, b), (b, c) and (c, a) is at the origin, then $a^3 + b^3 + c^3 =$
 a) 0 b) abc
 c) $3abc$ d) $-3abc$
57. The reflection of the point (4, -13) about the line $5x + y + 6 = 0$ is
 a) (-1, -4) b) (3, 4)
 c) (0, 0) d) (1, 2)
58. If the lines $x + q = 0$, $y - 2 = 0$ and $3x + 2y + 5 = 0$ are concurrent, then the value of q will be :
 a) 1 b) 2
 c) 3 d) 5
59. The equation of the line passing through (1, 5) and perpendicular to the line $3x - 5y + 7 = 0$ is
 a) $5x + 3y - 20 = 0$
 b) $3x - 5y + 7 = 0$
 c) $3x - 5y + 6 = 0$
 d) $5x + 3y + 7 = 0$
60. A line cuts off equal intercepts on the coordinate axes. The angle made by this line with the positive direction of x-axis is :
 a) 15° b) 120°
 c) 90° d) 135°
61. If one end of a diameter of the circle $x^2 + y^2 - 4x - 6y + 11 = 0$ is (3, 4) then find the coordinates of the other end of the diameter.
 a) (2, 1) b) (1, 2)
 c) (1, 1) d) none of these

62. A parabola $y^2 = 32x$ is drawn. From its focus, a line of slope 1 is drawn. The equation of line is :

- a) $y = x + 8$ b) $y = x - 4$
c) $y = x$ d) $y = x - 8$

63. The equation of the parabola which passes through (2, 3) and axis is along x-axis is :

- a) $2y^2 + 9x = 0$
b) $y^2 = 9x$
c) $2y^2 - 9x = 0$
d) $y^2 = -9x$

64. The length of the latus rectum of the ellipse $3x^2 + y^2 = 12$ is :

- a) 4 b) 3
c) 8 d) $\frac{4}{\sqrt{3}}$

65. The eccentricity of the hyperbola $4x^2 - 9y^2 = 36$ is :

- a) $\frac{\sqrt{13}}{3}$ b) $\frac{\sqrt{14}}{3}$
c) $\frac{\sqrt{15}}{3}$ d) $\frac{\sqrt{11}}{3}$

66. $\lim_{x \rightarrow 2} \frac{x^3 - 8}{x - 2}$ is equal to :

- a) 12 b) $-\frac{7}{3}$
c) -12 d) $\frac{7}{3}$

67. $\lim_{x \rightarrow 0} \frac{x}{\sqrt{1+x} - 1}$ is equal to :

- a) -2 b) $\frac{0}{0}$
c) 2 d) doesn't exist

68. $\lim_{x \rightarrow 0} \frac{2 \sin^2 3x}{x^2}$ is equal to :

- a) $\frac{2}{3}$ b) 2
c) -18 d) 18

69. $\lim_{x \rightarrow 0} \frac{e^x + e^{-x} - 2}{x^2}$ is equal to :

- a) -1 b) 1
c) 0 d) e

70. $\lim_{x \rightarrow a} \frac{\tan x - \tan a}{\sin a - \sin x}$ is equal to :

- a) $-\sec^3 a$ b) $\sec^3 a$
c) $\tan a$ d) $-\tan a$

71. $\frac{d}{dx} \left(\frac{x^2 + 1}{x} \right) = ?$

- a) $\frac{1}{x^2}$ b) $1 + \frac{1}{x^2}$
c) $1 - \frac{1}{x^2}$ d) $2 - x^2$

72. If $y = \frac{1}{a - z}$ then $\frac{dz}{dy}$ is :

- a) $-\frac{1}{(z - a)^2}$
b) $(z + a)^2$
c) $-(z - a)^2$
d) $(z - a)^2$

73. If $y = \frac{x+2}{x-2}$ then $y'(-2)$ is equal to :

- a) $\frac{1}{4}$ b) $-\frac{1}{4}$
c) 4 d) -4

74. The first order derivative of $\tan(4x-7)$ is :

- a) $-4 \sec(4x-7)$
b) $4 \sec^2(4x-7)$
c) $\sec^2(4x-7)$
d) none of these

75. $\lim_{x \rightarrow \pi} \frac{\tan x}{x - \pi} = ?$

- a) 1 b) -1
c) π d) 0

76. If $f(x) = \sin 2x - \cos 2x$, then $f\left(\frac{\pi}{6}\right) = ?$

- a) $-1 - \sqrt{3}$
b) $-1 + \sqrt{3}$
c) $1 + \sqrt{3}$
d) $1 - \sqrt{3}$

77. $\lim_{x \rightarrow -1} \frac{x^3 + 1}{x + 1}$ is :

- a) $\frac{0}{0}$ b) 1
c) -3 d) 3

78. $\frac{d}{dx} \operatorname{cosec} x = ?$

- a) $-\operatorname{cosec} x \cdot \cot x$
b) $\operatorname{cosec} x \cdot \cot x$
c) $\cot^2 x$
d) $-\cot^2 x$

79. If $f(x) = x^2 - 3x + 4$, then the value of x for which its derivative is zero:

- a) -3 b) $\frac{3}{2}$
c) 2 d) $\frac{1}{2}$

80. $\lim_{x \rightarrow -1} [1 + x + x^2 + x^3 + \dots + x^{10}]$

- a) $\frac{1}{2}$ b) 1
c) -1 d) doesn't exist

81. The mean deviation of the data : 3, 10, 10, 4, 7, 10, 5 is .

- a) 3 b) 2
c) 3.75 d) 2.57

On the basis of following table, answer the question no. 82 to 85 :

Marks	3	5	7	9	11	13
Number of students	6	8	15	25	8	4

82. What is the total number of students having marks not fewer than 9 ?

- a) 25 b) 37
c) 12 d) 54

83. Mean marks of students :

- a) 8 b) 7.5
c) 9 d) None of these

84. The value of $\sum f_i |x_i - \bar{x}|$, where rotations have their usual meanings :

- a) 136 b) 137
c) 138 d) 130

85. Mean deviation of the data given in table :

- a) 1.09 b) 2.0
c) 2.06 d) 2.09

86. The mean deviation of the data 3, 10, 10, 4, 7, 10, 5 is :

- a) 3 b) 2
c) 3.75 d) 2.57

87. Select the appropriate in

$$\sum_{i=1}^n (x_i - \bar{x})^2 = \sum_{i=1}^n x_i^2 + \dots$$

- a) $\sum_{i=1}^n x_i$ b) $\sum_{i=1}^n x_i^2$
c) $\frac{(\sum x_i)^2}{n}$ d) $n \sum_{i=1}^n x_i$

88. What is the range off the series 15, 18, 13, 16, 14, 13, 14, 19, 21

- a) 19 b) 8
c) 13 d) 21

89. The mean of the following data :

6, 5, 2, 4, 17, 8 is :

- a) 7 b) 8
c) 5 d) 5.5

90. The mean of 100 observations is 50 and their standard deviation is 5. The sum of squares of all the observation is :

- a) 50000 b) 250000
c) 252500 d) 255000

91. The modulus of $(3-4i)(-5+12i)$ is :

- a) -15 b) 17
c) 65 d) 12

92. How many two digit numbers are divisible by 4 ?

- a) 22 b) 21
c) 25 d) 24

93. The ratio in which the line segment joining $(-1, 1)$ and $(5, 7)$ is divided by the line $x + y = 4$ is :

- a) 1 : 2 internally
b) 1 : 2 externally
c) 2 : 1 internally
d) 2 : 1 externally

94. The equation of ellipse whose vertices are $(\pm 5, 0)$ and foci are $(\pm 4, 0)$ is :

a) $\frac{x^2}{7} + \frac{y^2}{16} = 1$

b) $\frac{x^2}{16} + \frac{y^2}{7} = 1$

c) $\frac{x^2}{9} + \frac{y^2}{25} = 1$

d) $\frac{x^2}{25} + \frac{y^2}{9} = 1$

95. The value of

$3 \sin \frac{\pi}{6} \cdot \sec \frac{\pi}{3} - 4 \sin \frac{5\pi}{6} \cdot \cot \frac{\pi}{4}$ is :

- a) -1 b) 0
c) 1 d) 2

96. Distance between the point $(-3, 7, -2)$ and $(2, 4, -1)$ is :

- a) $\sqrt{34}$ b) $\sqrt{43}$
c) $\sqrt{31}$ d) $\sqrt{44}$

97. The co-ordinates of points in the YZ-plane are of the form

- a) $(0, b, 0)$ b) $(a, 0, c)$
c) $(0, b, c)$ d) $(a, 0, 0)$

98. The image of (x, y, z) in XY-plane is :

- a) $(x, y, -z)$ b) $(-x, -y, z)$
c) $(x, 0, 0)$ d) $(0, y, z)$

99. Length of median through A of the triangle ABC, where A $(0, 0, 6)$, B $(0, 4, 0)$ and C $(6, 0, 0)$:

- a) 5 units
b) 6 units
c) 3 units
d) 7 units

100. The coordinates of the point where the line joining A $(3, 4, 1)$ and B $(5, 1, 6)$ crosses the xy-plane.

a) $\left(\frac{13}{5}, \frac{23}{5}, 1\right)$

b) $\left(\frac{-13}{5}, \frac{-23}{5}, 0\right)$

c) $\left(\frac{13}{5}, \frac{23}{5}, 0\right)$

d) $\left(\frac{13}{5}, 0, \frac{23}{5}\right)$

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